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# Leistungsfähigkeit von elektronischen Entzerrern in hochbitratigen optischen Übertragungssystemen

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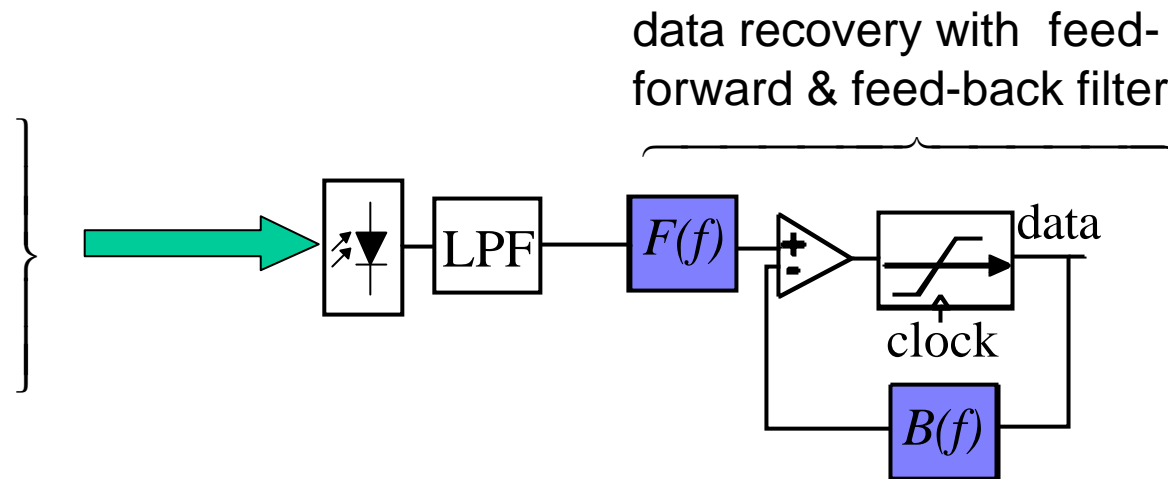
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## Outline

1. Motivation
2. Overview of Impairments: Chromatic Dispersion & SPM and PMD
3. Nonlinear Signal Components within electrical receiving Signal
4. Electronic equalizer approaches
5. Adaptive realization
6. Experimental results for Chromatic dispersion & SPM
7. Results for PMD
8. Summary

## Why Electronic Equalization?

- chromatic dispersion
- PMD
- nonlinear effects



application:

- compensate for dispersion and nonlinear effects
  - in WDM-links with DCF to compensate for residual dispersion
  - in the nonlinear power regime of the fiber
- compensate for PMD+GVD+SPM **independent from physical origins**
- standard **adaptive** algorithm available

in general **less cost intensive** than optical compensator

hardware implementation on **receiver-IC** combined with clock & data recovery

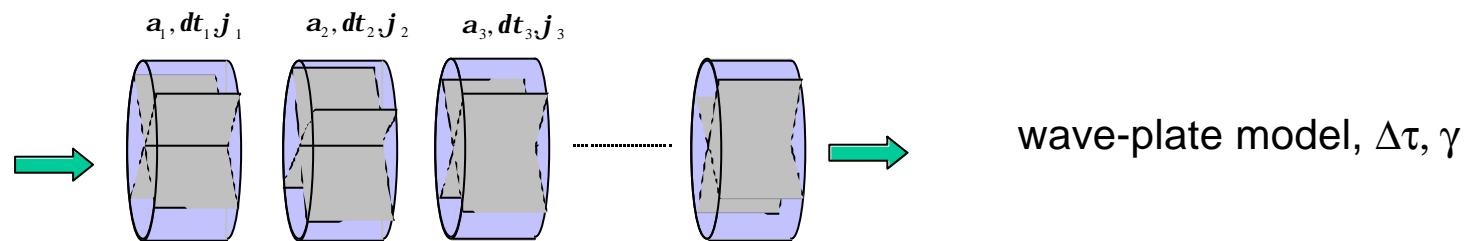
## Fiber Impairments

- **chromatic dispersion (GVD)** (Pulse broadening due to group velocity dispersion, square dependence)

$$H(f) \approx \text{const} \cdot e^{j2\beta \frac{D1L}{2c} f^2}$$

D=17ps/nm km for SSMF

- **polarization mode dispersion (PMD)** (differential group delay, mode coupling)

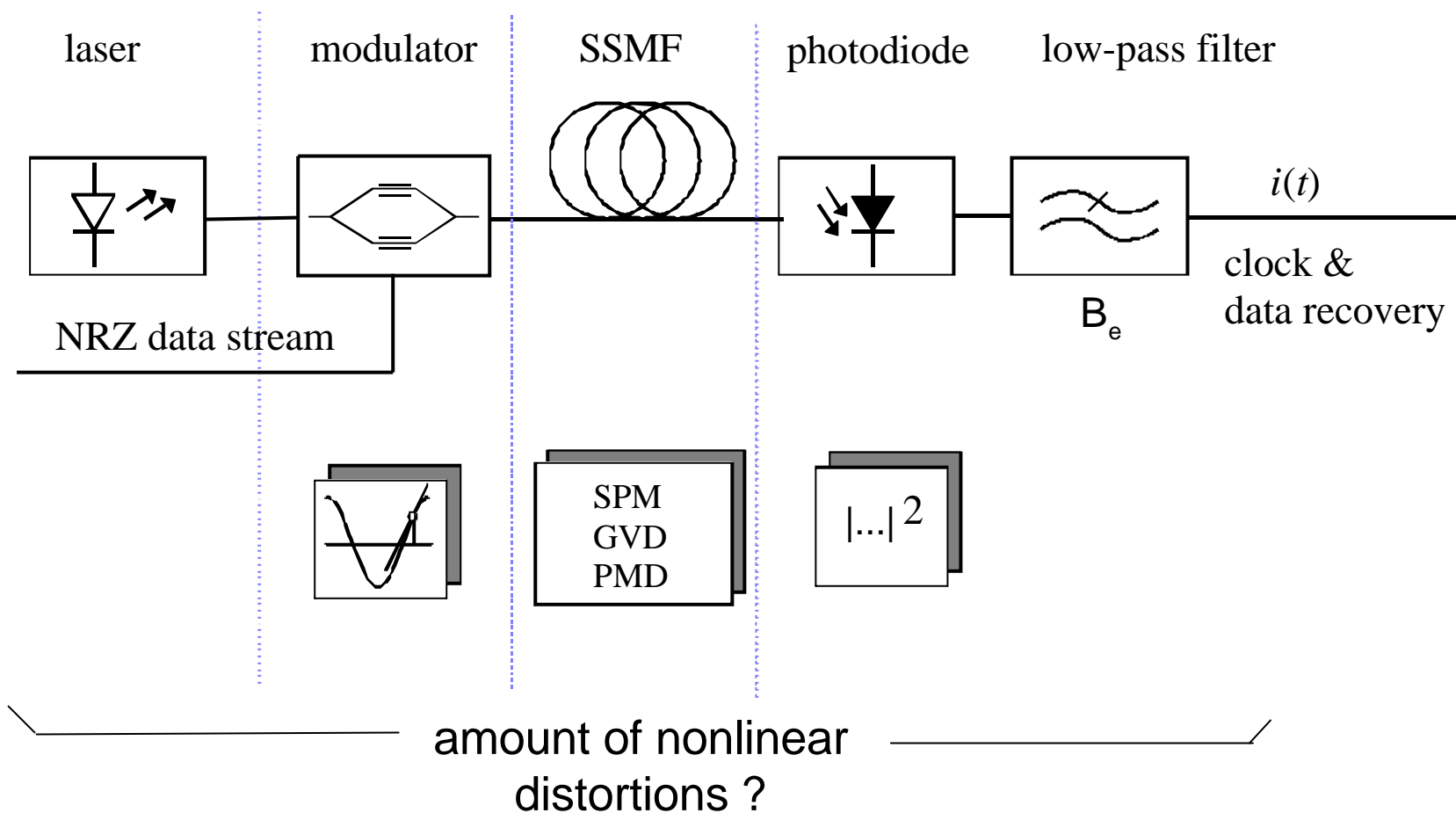


- **self phase modulation (SPM)**

$$\frac{\partial A}{\partial z} + \frac{\alpha}{2} A - j \frac{\beta_2}{2} \frac{\partial^2 A}{\partial t^2} = -j\gamma |A|^2 A$$

nonlinear Schrödinger-equation

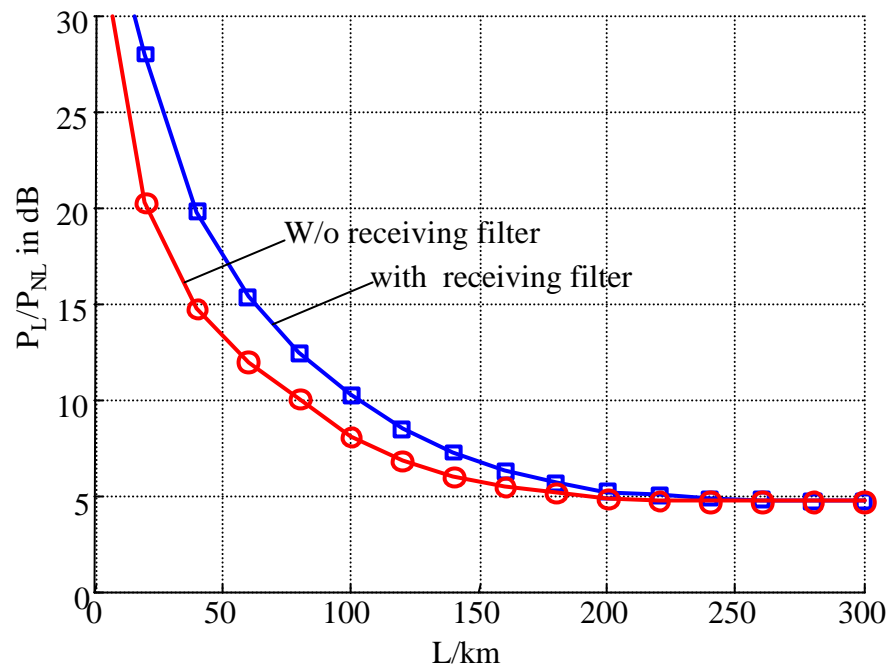
# Optical Single Channel Transmission System



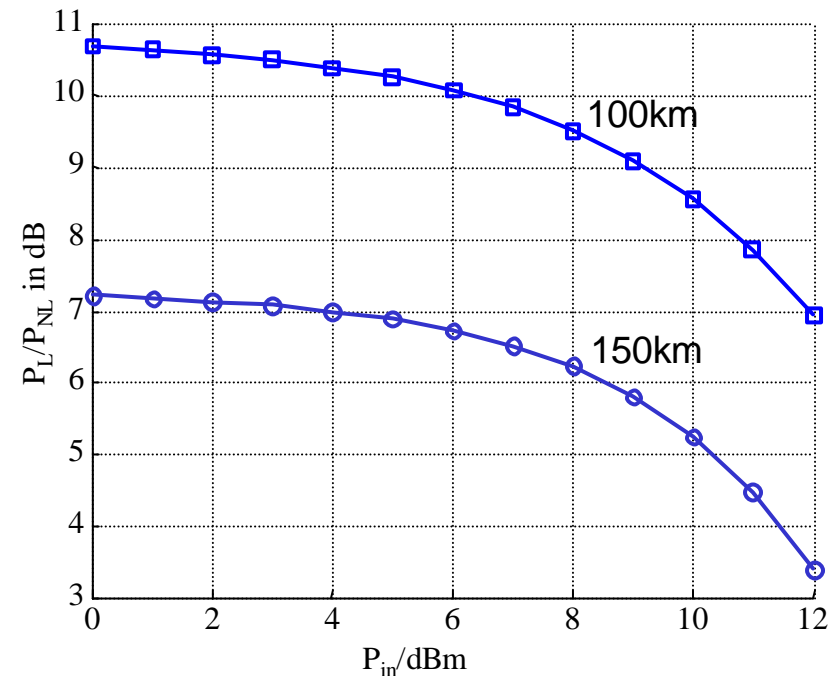
# Nonlinear Signal components within the electrical receiving signal for GVD and SPM

Volterra-series model:  $y_{receive}(t) = y_{linear}(t) + y_{nonlinear}(t)$

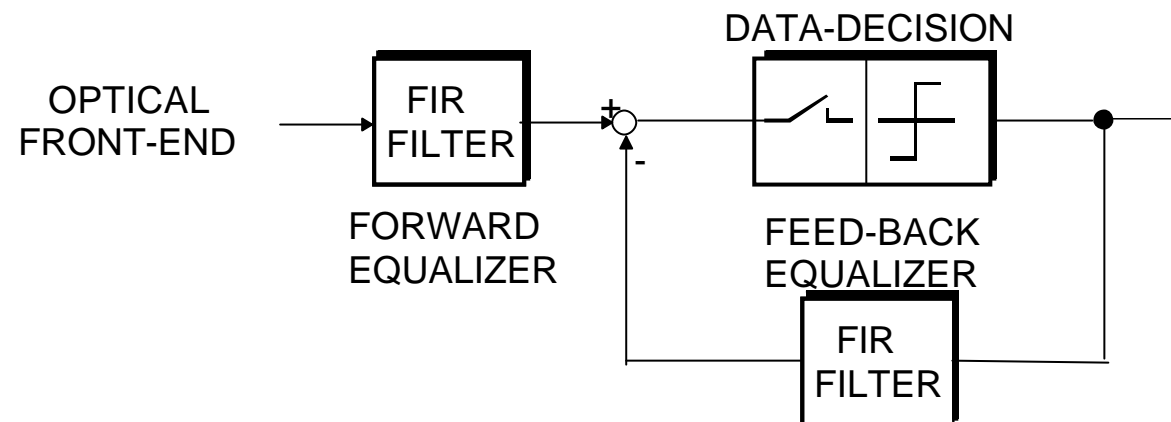
Ratio of linear signal components to nonlinear signal components vs. fiber length (17ps/nm/km) for linear fiber behavior



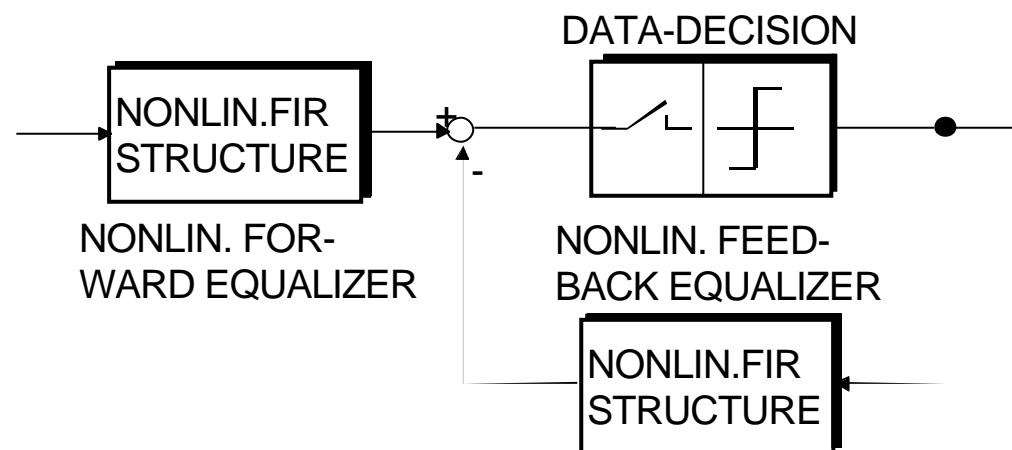
Ratio of linear signal components to nonlinear signal components vs. mean optical input power at 100&150km



## Electronic Equalizer Approaches

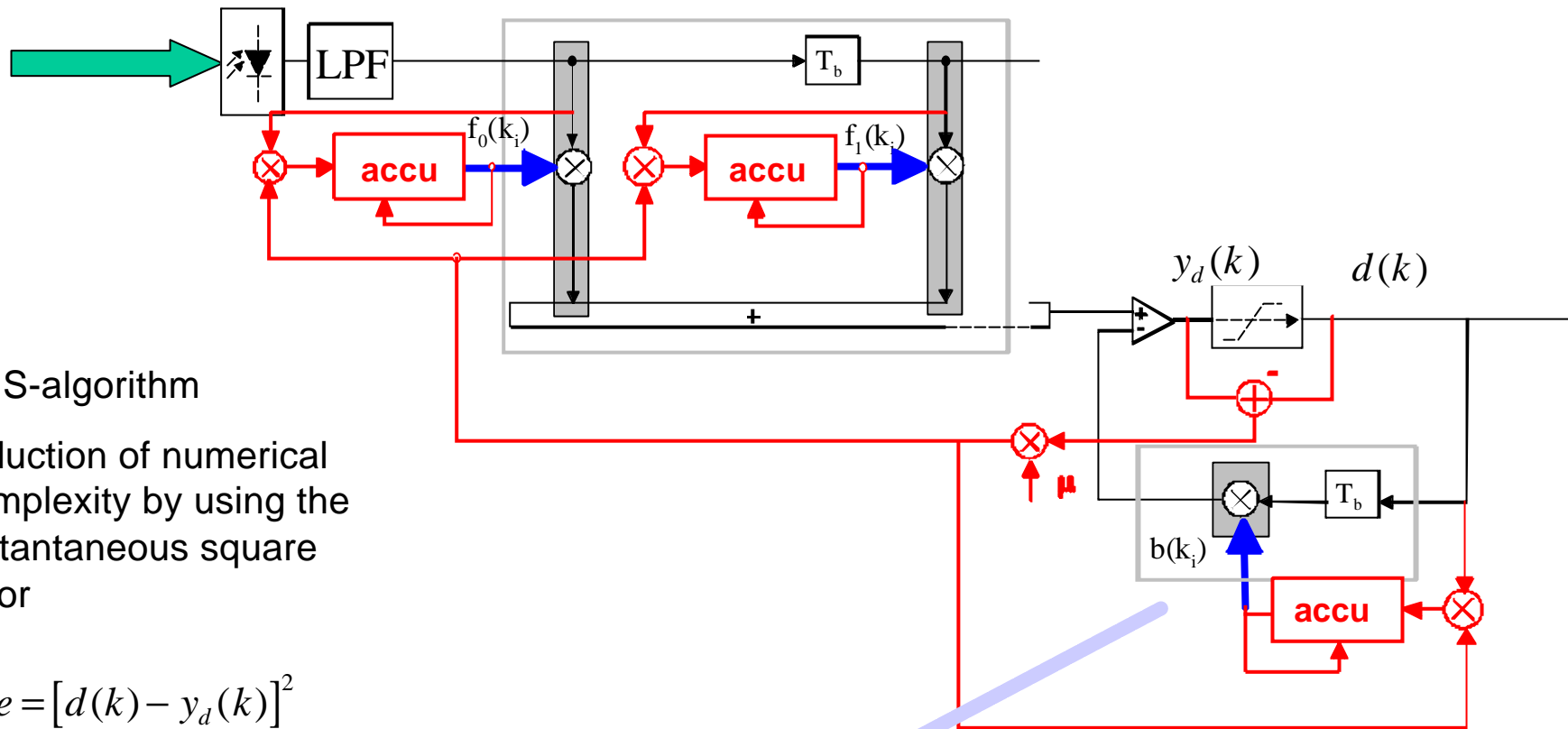


**FIR-DFE:** feed-back & feed-forward filter in order to compensate for precursor ISI



**NL-FIR-DFE:** nonlinear processing based on Volterra theory within forward and backward branch in order to compensate for nonlinear distortions

# Adaptive Equalizer Implementation (LMS-algorithm)



LMS-algorithm

reduction of numerical complexity by using the instantaneous square error

$$se = [d(k) - y_d(k)]^2$$

as a figure to minimize resulting in a simplified expression for the gradient

$$b(k+1) = b(k) + \underbrace{\mu}_{\text{weighting factor}} \underbrace{d(k-1)}_{\text{eq.state}} \underbrace{[d(k) - y_d(t_0 + k)]}_{\text{error}}$$

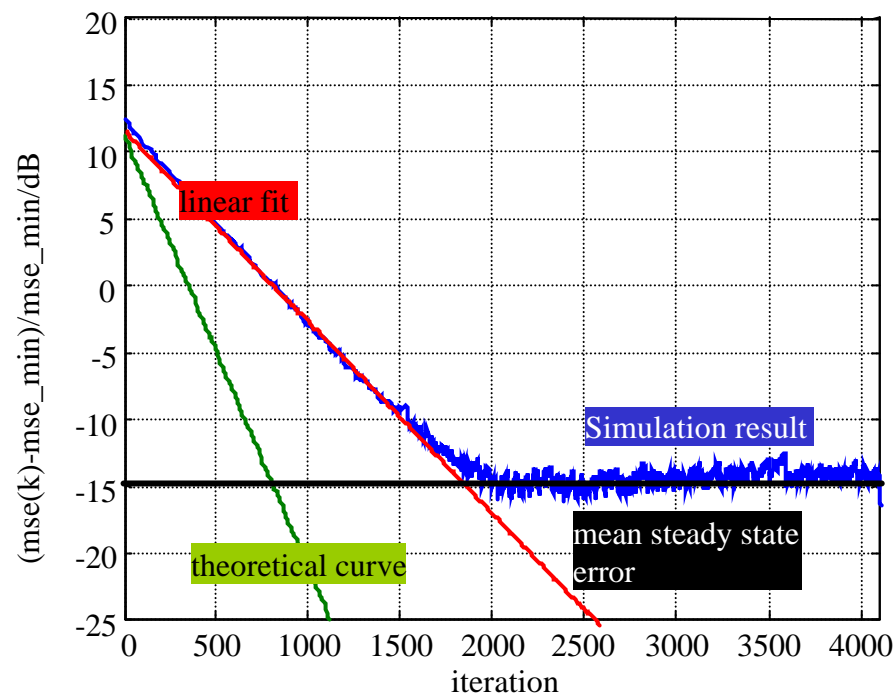
Steven Otto, ET & Telekomm., S. 11, 2001, 8



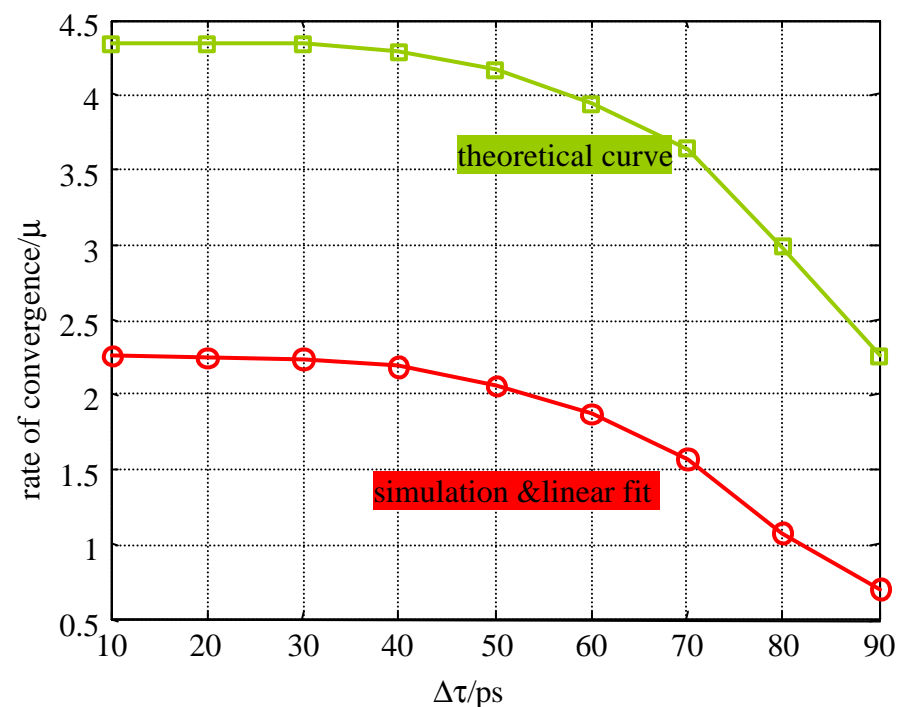
# Properties of LMS-Adaptation Process

Comparison between theoretical and simulated acquisition behavior of a 2 tap synchronous equalizer under first order PMD distortions

Residual error vs. number of iterations at  $\Delta\tau=80\text{ps}$



Convergence rate vs. DGD

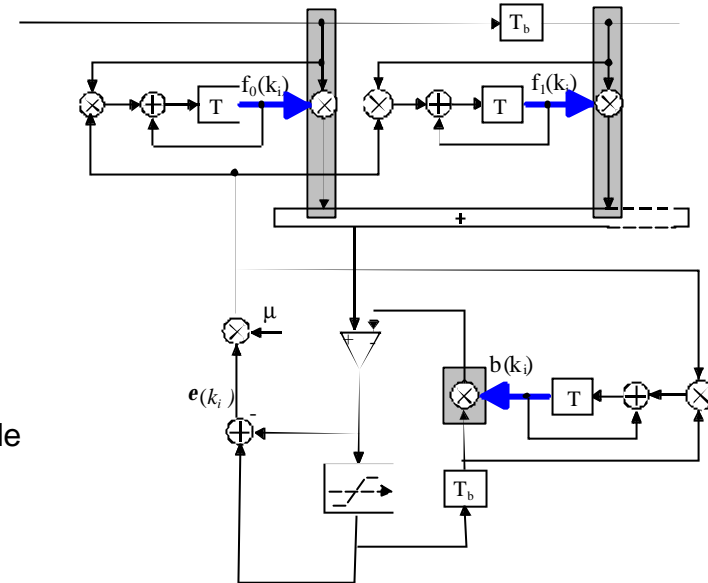
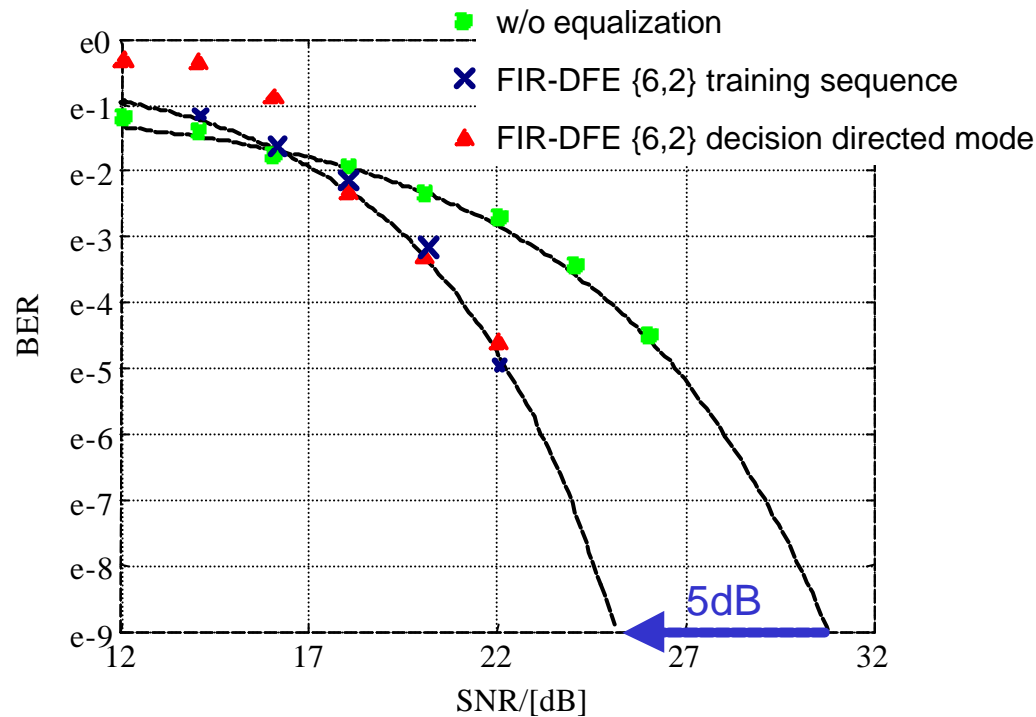


# Acquisition behavior of LMS algorithm

Monte-Carlo simulation

$$\text{DGD} = 0.8T_b, \gamma = 0.5$$

equalizer: FIRDFE  $\{6,2\}$ ,  $f_3=1$ ,  $f_i=0$ ,  $b_{1,2}=0$



acquisition requirements:  
 $EO > 15\%$   
 $BER < 10^{-2}$

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## Measurements

### Equalizer:

Prototype implementation (cooperation partner) of a Fractionally spaced equalizer with 10 coefficients and LMS-based adaptive coefficient setting

### Performance evaluation

Experiments were carried out in the lab at the chair for communications in Kiel (10Gb/s)

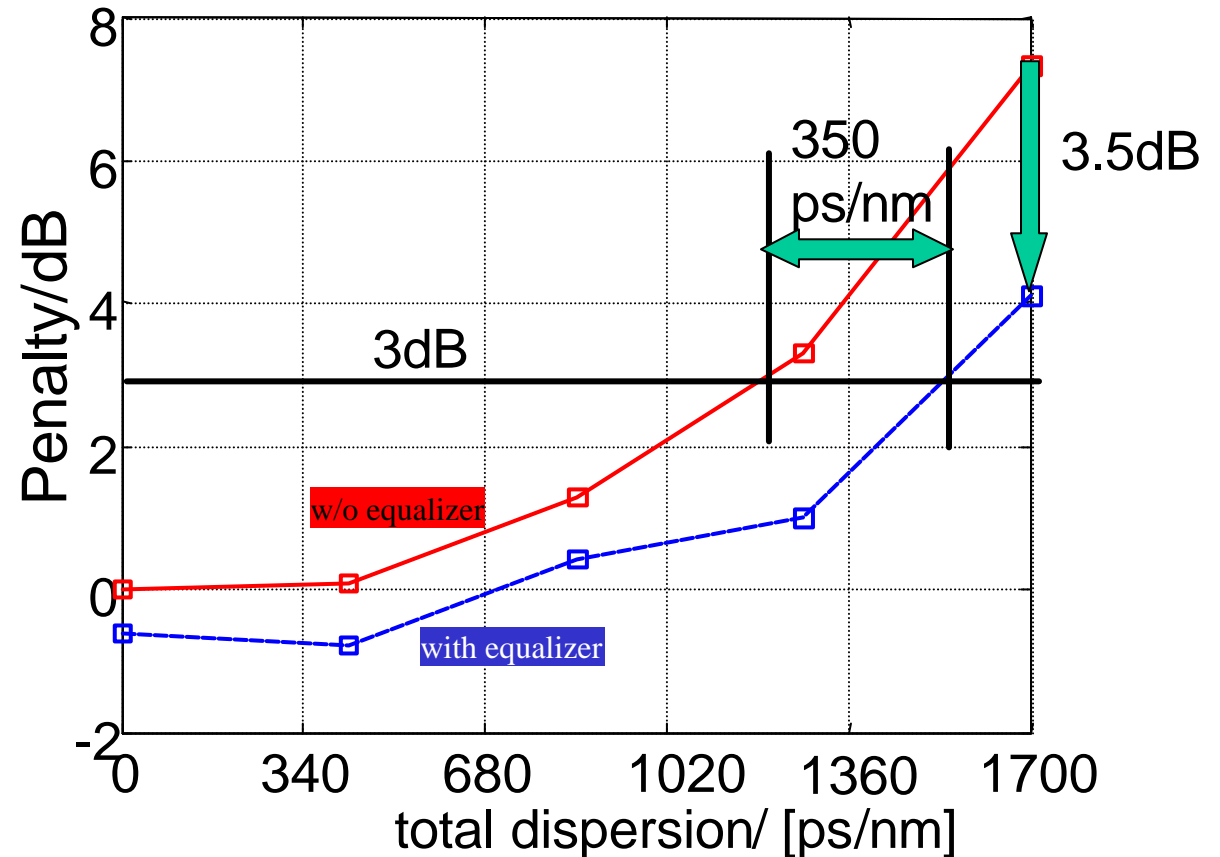
# Measurement Results for GVD

uncompensated link with linear fiber behavior and  $D=17\text{ps/nm/km}$

Decreased sensitivity against residual dispersion @3dB PP: 350ps/nm

improvement in maximal transmission distance @ 3dB PP: 20km

Power Penalty reduction @L=100km: 3.5dB

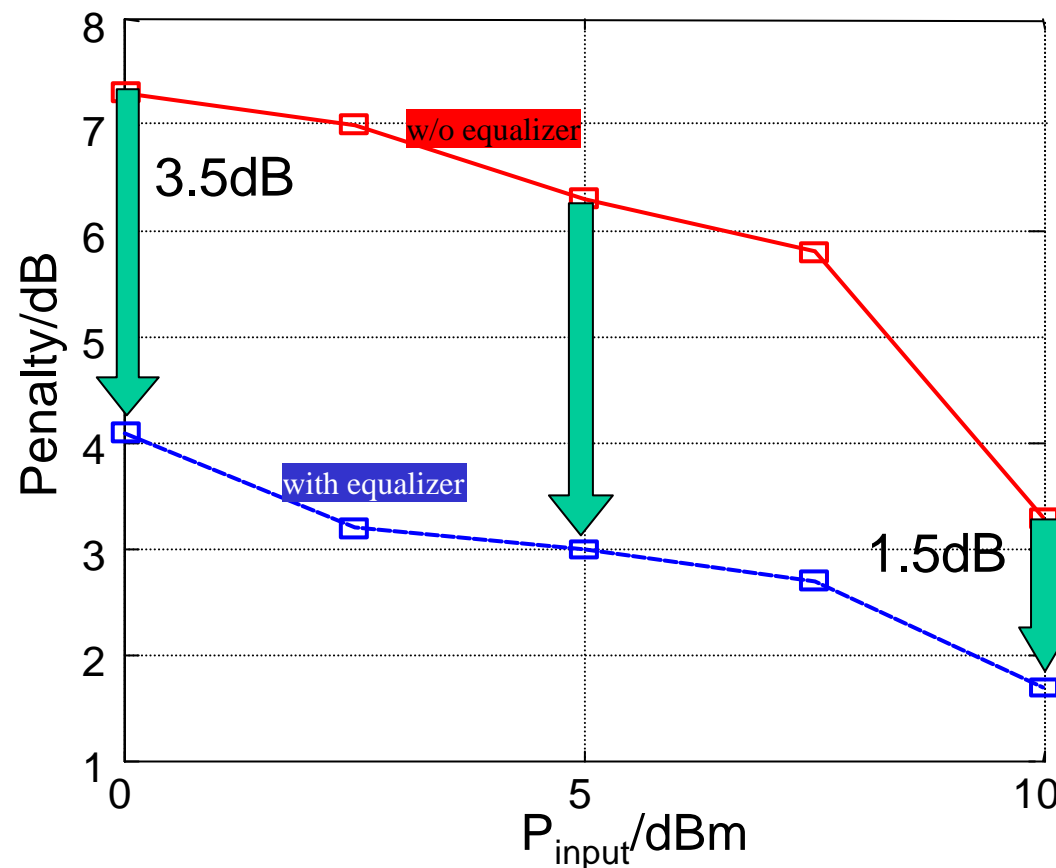


## Measurement Results for SPM

uncompensated link with high optical input power, 1700ps/nm (L=100km)

SPM effect causes additional nonlinear signal components within electrical receiving signal

Power Penalty reduction decreases from 3.5dB w/o SPM to 1.5dB with an considerable impact of SPM



# Simulation Results for PMD

PMD parameter:

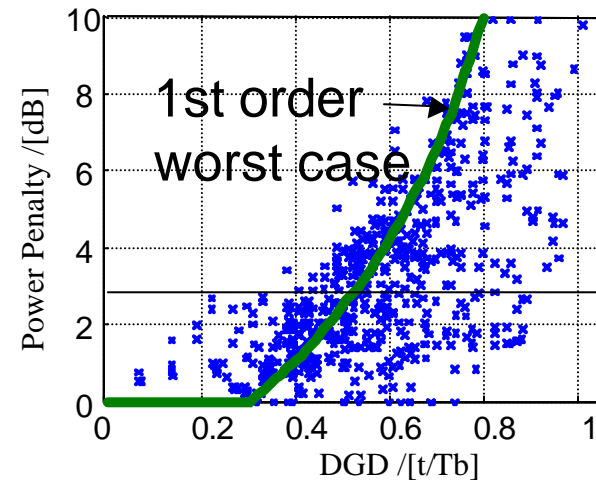
mean DGD value = PMD =  $0.5T_b$

# wave plates = 100

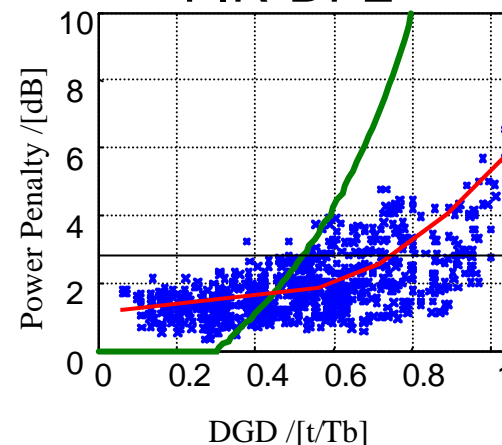
assuming an outage probability of  $10^{-5}$  (5min/year) a tolerable DGD of  $\Delta\tau$  corresponds to  $\text{PMD} = \Delta\tau / 3.2$

DGD		PMD
$0.3T_b$	→	<b><math>0.1T_b</math></b> w/o
$0.6T_b$	→	$0.2T_b$ FIR-DFE
$0.9T_b$	→	<b><math>0.3T_b</math></b> NL-FIR-DFE

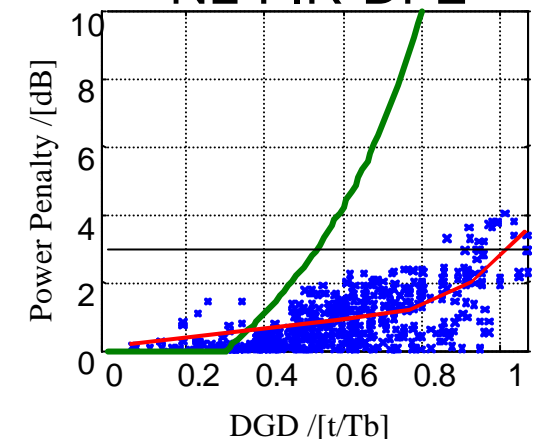
w/o equalization



FIR-DFE



NL-FIR-DFE



## Summary of Results and Conclusions

PMD						
$PMD/\sqrt{L}$	Maximum transmission distance in km at 10Gb/s			Maximum transmission distance in km at 40Gb/s		
	w/o equalization	FFIRDFE	NLFIRDFE	w/o equalization	FFIRDFE	NLFIRDFE
0.1	10000	40000	90000	625	2500	5625
2	25	100	225	1.56	6.25	14

GVD/SPM						
$P_{input}$ in dBm	Dispersion tolerance in ps/nm at 10Gb/s			Dispersion tolerance in ps/nm at 40Gb/s		
	w/o equalization	FFIRDFE	NLFIRDFE	w/o equalization	FFIRDFE	NLFIRDFE
0	1200	1800	1800	80	140	150
10	1000	1750	1500	-	-	-

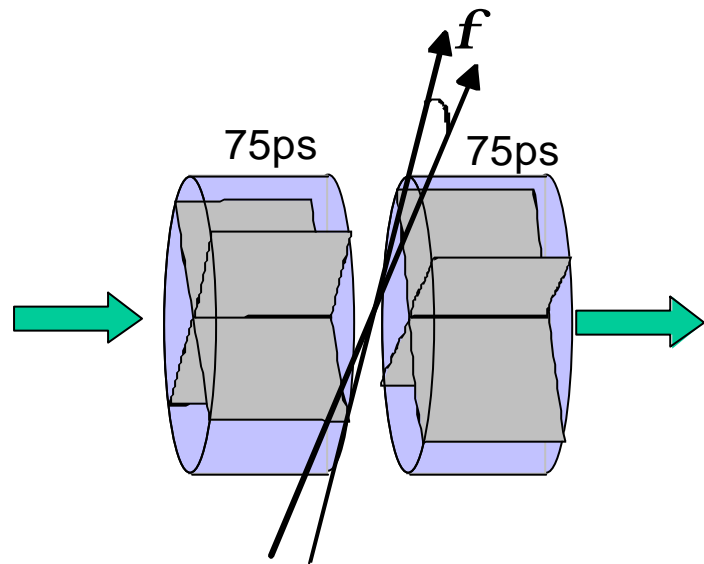
## Project summary so far

- A Volterra-Theory model has been developed which enables a theoretical performance analysis of electronic equalizer in optical transmission systems
- A complete performance evaluation including adaptation algorithm properties were performed on a simulation basis at 10Gb/s and 40Gb/s for GVD, SPM and PMD
- Experimental Performance evaluation at 10Gb/s in cooperation with an industry partner

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# Nonlinear Signal components within the electrical receiving signal for a 2 section PMD-model



Nonlinear components vanish if 2<sup>nd</sup> order coefficient vanishes.

That is either if

- fast/slow** axis coincide with **fast/slow** axis
- or
- fast/slow** axis coincide with **slow/fast** axis

